



## **COLLAPSE ANALYSIS OF A REINFORCED CONCRETE FRAME DUE TO MIDDLE COLUMN LOSS BY EXPLOSION**

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### **Abstract**

The subject of the overall structural collapse under hazardous loads in reinforced concrete frames has been addressed in various research. However, most of those studies have examined the column removal scenario where one of columns is removed and the load of this column is applied vertically on the upper face to assess the behavior of the frame until failure. One of the shortcomings of the previous mechanism is that it neglects the main reason for the failure of the column and the impact of that reason on the different elements of the structure.

The current work presents a numerical investigation of frame collapse as a result of sudden column failure due to an explosive wave. The frame of study has already been tested in a previous work of the author. It was a reinforced concrete frame that has been cast without an intermediate column and then dynamically loaded in the position of the missing column until collapse. In this study, the behavior of that frame is re-evaluated under the effect of instantaneous removal of the middle column due to explosion loads. Analysis was performed using Abaqus software where frame capacity and failure mode were monitored considering different locations of application of incident wave on the target column. Comparing the obtained results with the original model indicated that both capacity and mode of failure differ significantly by changing the location of application of incident wave.

**Key Words:** Explosion impulse load; reinforced concrete frame; finite element analysis; capacity, failure pattern

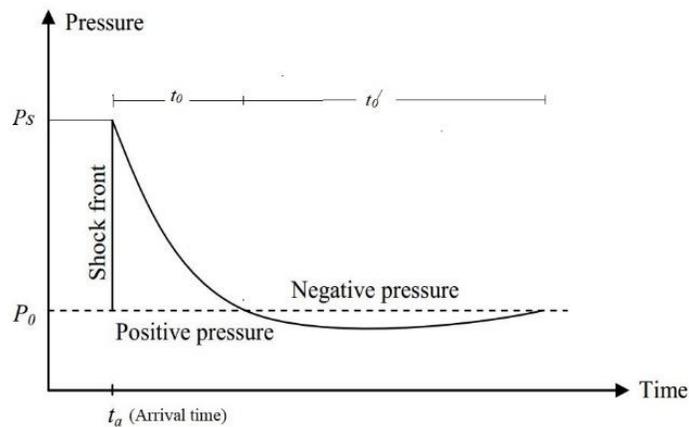
### **1. Introduction**

Progressive collapse, as described in American Society of Civil Engineers (ASCE) standard 7-05, is the spread of an initial local failure from element to element, eventually resulting in the collapse of an entire structure or a disproportionately large part of it. To occur, progressive collapse needs abnormal loading to initiate damage as well as a structure that lacks adequate continuity, ductility, and redundancy. With repeated catastrophic collapses of many buildings around the world, many research activities have led to more detailed guidelines on preventing progressive collapses (e.g. [1–3]). A literature survey on the currently used methodologies to avoid progressive collapse is found in [4-9]. Besides, several research papers have been published presenting both experimental and numerical analysis of progressive collapse in reinforced concrete frames. For example, Brunesi et al [10] developed fragility functions for low-rise reinforced concrete (RC) framed building structures to be implemented in progressive

collapse risk assessment. Two building classes representative of European buildings designed for gravity loads and earthquake resistance in accordance with Eurocodes, were investigated in the study. Fam and Tan [11] carried out a series of dynamic tests on two-dimensional reinforced concrete beam-column frames simulating the sudden removal of a supporting column via a quick-release device. Weng et al [12] traced the collapse sequence of the progressive collapse process using a member removal algorithm based on combined flexural/shear/axial failure criteria. Brodsky and Yankelevsky [13] evaluated the possible contributions of infill masonry walls to prevent progressive collapse. Weng et al [14] tested three scaled moment-resisting RC frames to validate the proposed flexural and axial damage criteria. In addition, three shear-dominant damaged tests were also modeled by authors to assess the proposed shear damage criteria. Lu et al [15] conducted laboratory progressive collapse tests of five 1/3- scaled RC frame substructure specimens subject to an edge-column-removal scenario.

In the research presented above, most studied frames have either been cast without a column or the column has been suddenly removed during the test without a dynamic load. However, the main reason of column collapse will certainly have a different effect on the overall structural behavior.

Between the various abnormal events, explosions have recently become a major cause of structural collapses due to terrorist threats around the world. Explosion is an instantaneous release of energy resulting in a fast increase in pressure. From the explosion, a wave front is formed and spreads spherically. The temperature and pressure resulting from explosion decrease with increasing distance from the center of detonation. After a few milliseconds the whole process is over, and the pressure returns to atmospheric pressure,  $P_0$ . The typical pressure profile of the explosion wave in time for the explosion in the air is given in Figure (1). At the time of arrival,  $t_a$ , there is an immediate increase in pressure followed by the positive and negative phases. A simplification of the shock wave is often made to make it easier to describe the load that the wave will give rise to. Usually, the negative phase is neglected and the positive pressure is considered as a critical case.



**Figure (1):** Pressure-time profile of the explosion wave

The specific wave impulse,  $i_s$ , that is equal to the area under the pressure-time curve from the moment of arrival,  $t_a$ , to the end of the positive phase and is given by expression:

$$i_s = \int_{t_a}^{t_a+t_0} P_s(t) dt \quad (1)$$

Based on earlier numerical and experimental studies, many empirical expressions were proposed to calculate Peak static wave front overpressure,  $P_s$ , for example, Brode [16] suggested the following equations:

$$P_s = \frac{6.7}{Z^3} + 1 \quad \text{For } P_s > 10\text{bar}$$

$$P_s = \frac{0.795}{Z} + \frac{1.455}{Z^2} + \frac{5.58}{Z^3} - 1.019 \quad \text{For } 0.1 < P_s < 10\text{bar}$$

(2)

Newmark and Hansen [17] proposed the following:

$$P_s = 6874 \frac{W}{R^3} + 93 \sqrt{\frac{W}{R^3}} \text{ bar}$$

(3)

And Mills [18] proposed the following:

$$P_s = \frac{108}{Z} + \frac{114}{Z^2} + \frac{1772}{Z^3} - 1.019 \text{ kPa}$$

(4)

Where,

Z: Scaled distance,  $Z = \frac{R}{\sqrt[3]{W}}$

(5)

R: Distance from the center of a spherical charge, m

W: Charge mass expressed in kilograms of TNT.

There is an ongoing effort by researchers to study the influence of the explosions on the various structural elements to develop design methods that lead to better performance under such load condition. (See for example [19-25] for slabs, [26-31] for columns and [32-34] for beams).

In the current research, it is intended to link both successive collapse and explosion loads by providing a numerical study of a frame under the influence of the collapse of one of its columns due to an explosive wave.

## 1 Description of the studied frame:

The structure considered in the current study is a two-bay one-story reinforced concrete frame denoted as “FR (1)” in figure (2). This frame is the front one of two successive frames linked by three secondary beams and having the dimensions and reinforcement details shown in figures (2) and (3). According to laboratory tests, the compressive strength of concrete was 42Mpa while the tensile strength of longitudinal steel bars and stirrups were 345 and 250Mpa respectively. FR (1) was intentionally cast without the intermediate column and formerly tested by loading it dynamically at the position of the removed column until failure to investigate its behavior and capacity under column loss condition [35]. Figure (4) shows test setup of the frame. During the test, the frame was loaded at a rate of 1t/sec and the capacity of the frame reached 60.5 kN.

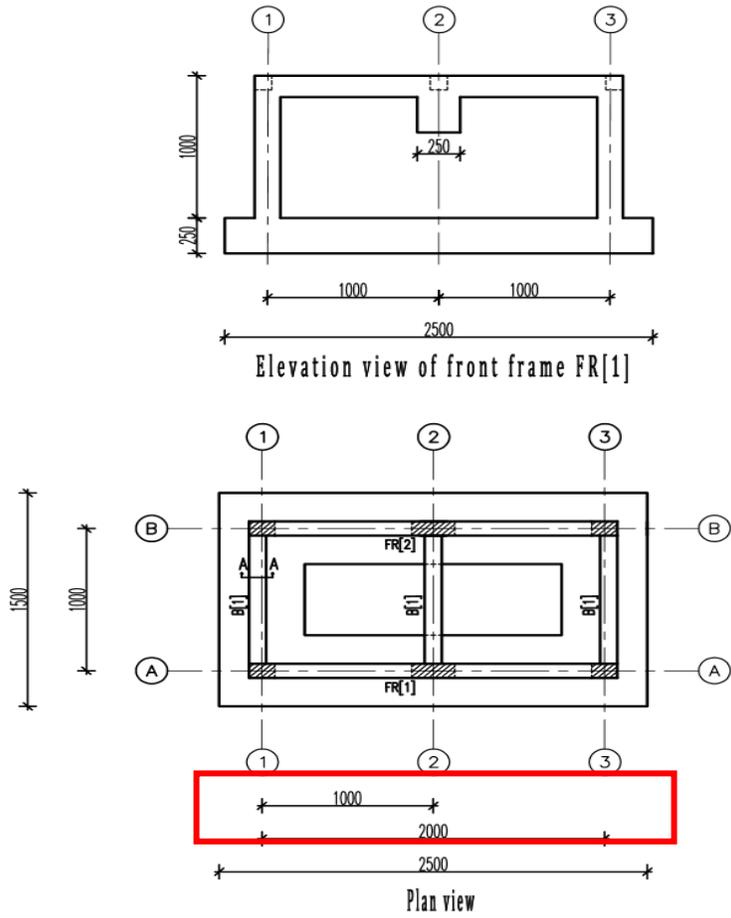


Figure (2): Dimensions of studied frame (Dimensions in mm)

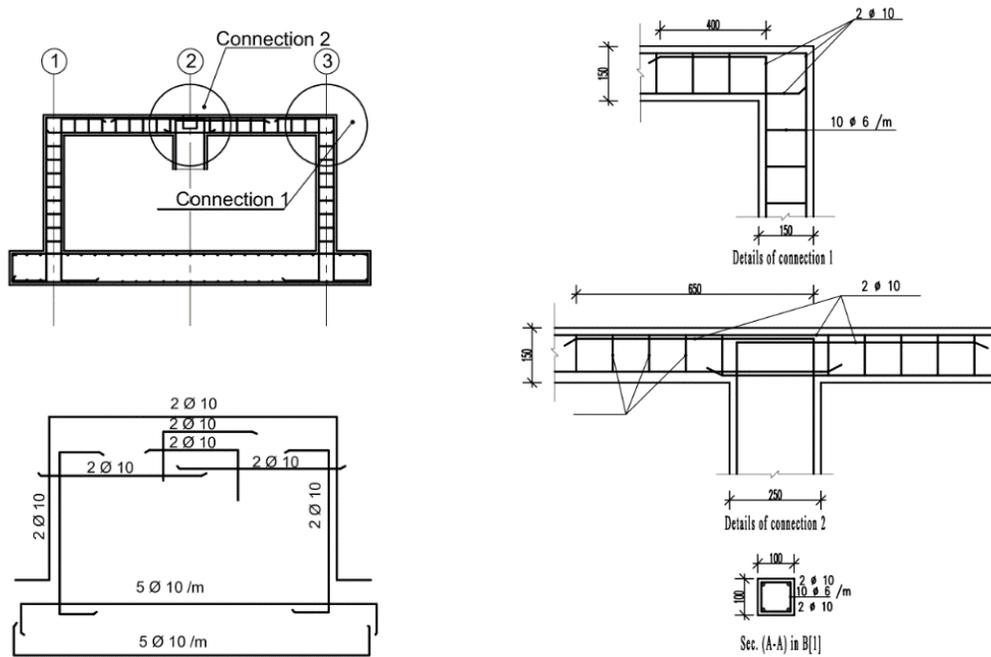


Figure (3): Reinforcement detailing of the studied frame (Dimensions in mm)



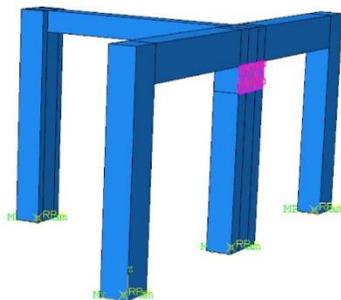
Figure (4): The frame of study as per [35]

## 2 Objective of the research:

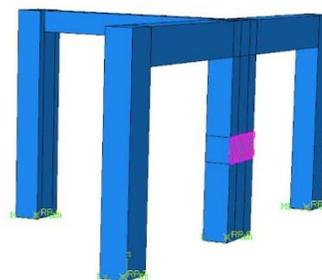
In the current research, the finite element package, Abaqus, is used to conduct dynamic nonlinear analyses of the previous frame to re-evaluate its behavior if the middle column collapsed due to an explosion incident wave. The main aim here is to compare both load-deflection curves and failure patterns of the frame if it was cast from the beginning without a column and if the column exists and then collapsed due to an explosion. In addition, the influence of the location where explosion is applied on the column is studied.

To achieve this goal, a numerical model representing the tested frame was presented and verified against the tested one. Then, the formerly removed column was added to the verified numerical model and loaded by 150 kN distributed as a pressure load on its upper surface. The column was then exposed to a large amount of TNT leading to its total collapse. After column failure, the 150-kN load, carried up to that time by the column, began to transfer to the frame resulting in a progressive collapse.

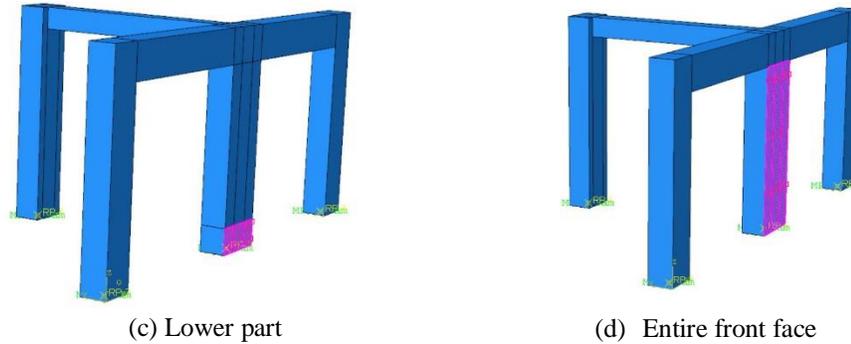
Four different positions of incident wave action on column were considered in the analysis: the upper part, the middle part, the bottom part as well as the entire front surface of the middle column. In the former three cases, the explosion load was assumed to be acting on an area of  $12 \times 25$  cm of the column front surface. Figure (5) sums the different locations considered in the analysis.



(a) Upper part



(b) Middle part



**Figure (5):** Different locations of application of explosion load on the middle column

### 3 Finite element model:

Two models were built in Abaqus; a model without the middle column to represent the experimental one “denoted here as Model (1)”, and a model with the middle column that will be exposed to instantaneous collapse due to explosion “denoted here as Model (2)”. In both models, the concrete was modelled using reduced order eight-node solid element, C3D8R. The reinforcement bars were modelled as truss elements that were embedded in concrete. Abaqus concrete damaged plasticity model was used to represent concrete material. The dynamic increase factors for compressive and tensile strengths of concrete under high rates of loading, based on test results, were calculated based on the CEB model code [36] and were found to be 1.67 and 2.2 for compression and tension respectively. The main parameters needed to define the concrete model after computation of failure compression and tension strength at high strain rates are summarized in table (1) while figure (6) displays the compressive and tension behavior of concrete at static and dynamic loads. Rebar material was modelled using Abaqus elastic-plastic model. The main parameters used to define the reinforcement material for both longitudinal bars and stirrups are listed in table (2).

Although FR (1) is the objective in the study, the transverse beam (B1) at the location of loading has been added to the numerical model to study the participation of column (B-2) in the maximum frame capacity after the column collapse in the different considered situations.

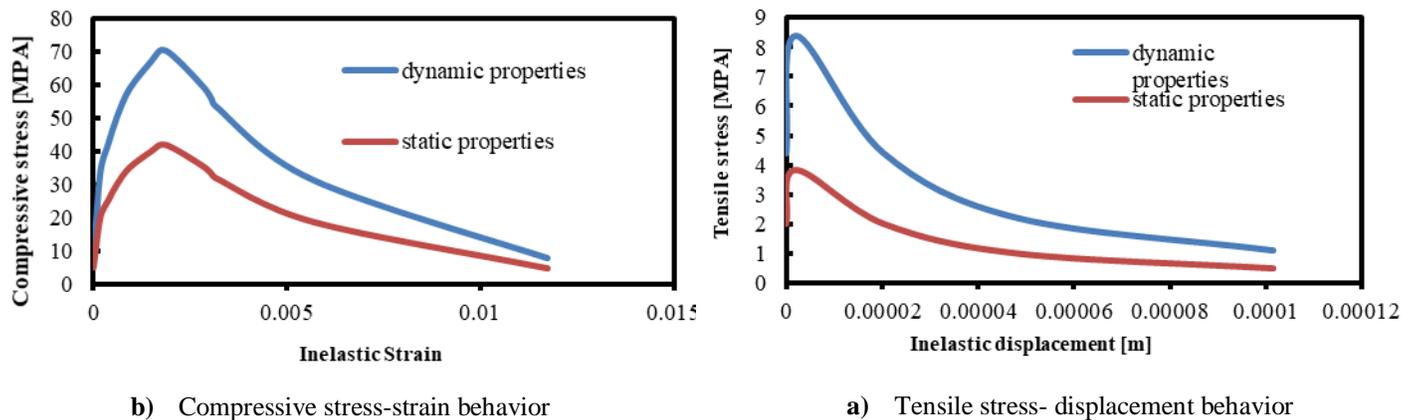
**Table (1):** Data defines concrete material

Density (kg/m <sup>3</sup> )	2570
Young's Modulus: $E$ (MPa)	25,200
Poisson's ratio	0.2
Dilation angle	20
Yield stress in compression (MPa)	8.4
Compressive ultimate stress (MPa)	70.5

Inelastic strain	0.00178
Failure stress in compression (MPa)	7.8
Strain at failure	0.0056
Ultimate tensile stress (MPa)	8.4
Tension stiffening	$2 \times 10^{-6}$

**Table (2):** Data defines longitudinal and stirrups steel material.

	Longitudinal steel	Stirrups
Reference density (kg/m <sup>3</sup> )	7800	7800
Young's Modulus, E (MPa)	200,000	200,000
Tensile Strength, $f_t$ (MPa)	345	250



**Figure (6):** The compressive and tension behavior at static and dynamic load.

#### 4

#### Applying explosion on Abaqus/Explicit:

The loading effects due to an explosion in air were defined in Abaqus/Explicit by the CONWEP model. This model uses a scaled distance,  $Z$ , based on the distance of the loading surface from the source of the explosion and the amount of explosive detonated. For a given scaled distance, the model provides the following empirical data: the maximum overpressure (above atmospheric), the arrival time, the positive phase duration, and the exponential decay coefficient for both the incident pressure and the reflected pressure. Using these parameters, the entire time history of both the incident pressure and reflected pressure can be constructed. The total pressure  $P(t)$ , on a surface due to the blast wave is a function of the incident pressure,  $P_{incident}(t)$ , the reflected pressure,  $P_{reflected}(t)$ , and the angle of incidence,  $\theta$ , which is defined as the angle between the normal of the loading surface and the vector that points from the surface to the explosion source [37]. The total pressure is defined as:

$$P(t) = P_{incident}(t)[1 + \cos\theta - 2\cos^2\theta + P_{reflected}(t)\cos^2\theta] \text{ for } \cos\theta \geq 0,$$

$$P(t) = P_{incident}(t) \text{ for } \cos\theta < 0$$

(6)

In Abaqus model, the air blast was defined in interaction module. Based on several trails, the amount of explosive material required to cause failure of column was found to be 100kg of TNT. The source point was assumed at 1meter far away from the center of the target surface of the column.

In the model, a vertical pressure was applied on the middle column using an amplitude curve where load gradually increased from zero to 150 kN in 0.007s. This was found to be the minimum period needed to make the middle column fully loaded by load before applying incident wave, i.e. the time required for the load to reach supports. The load was then kept constant with time till the end of analysis. After 0.007s, the bomb of 100kg TNT was exploded. The applied pressure and source of detonation are shown in figure (7) while figure (8) shows the incident wave due to detonation of 100 kg TNT applied at 1 meter away from the middle column. The incident wave reached column surface after 0.00025 s of the detonation with maximum pressure of  $1.06 \times 10^5$  Pa. this pressure was rapidly decreased in an exponential manner as shown in figure.

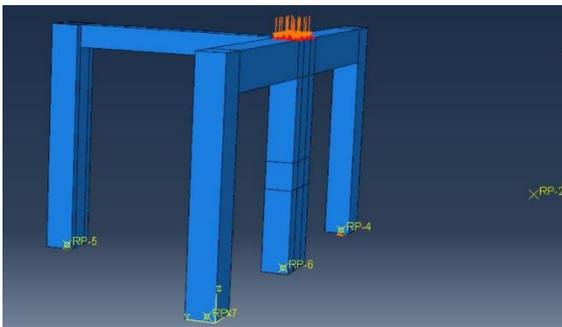


Figure (7): The applied load and source of detonation

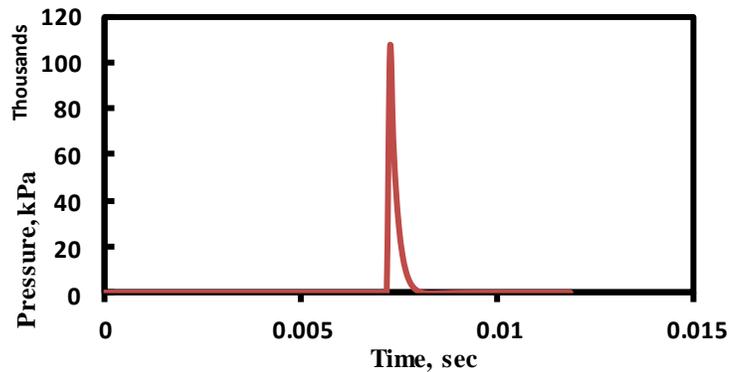


Figure (8): The incident wave due to detonation of 100 kg TNT

## 5

### Analysis results and discussion

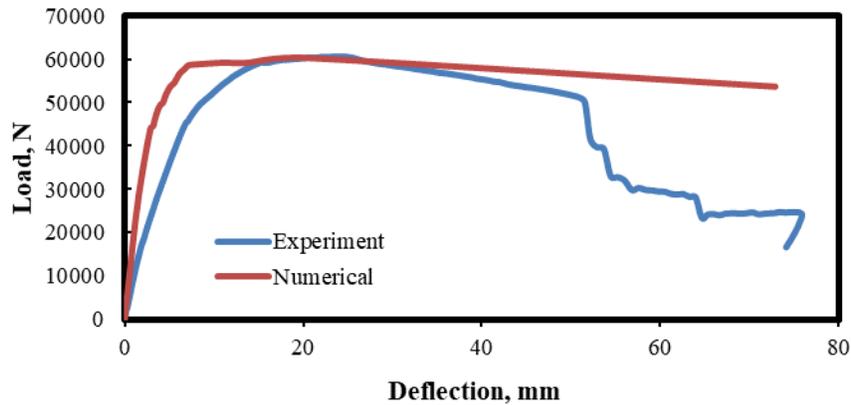
#### 5.1 Comparison between model (1) and experimental results

Figure (9) compares the failure modes in the tested frame and Model (1). It is clear that the shape of collapse is identical in both experimental model and numerical Model (1) where the collapse occurred beside connection 1 and at connection 2 in one side.

The load- deflection relationships is also plotted in figure (10) which shows fair agreement where the maximum capacity in the tested frame reached 60.5 kN at deflection 24 mm while in Model (1) the capacity is 60.25 kN at 20 mm deflection.



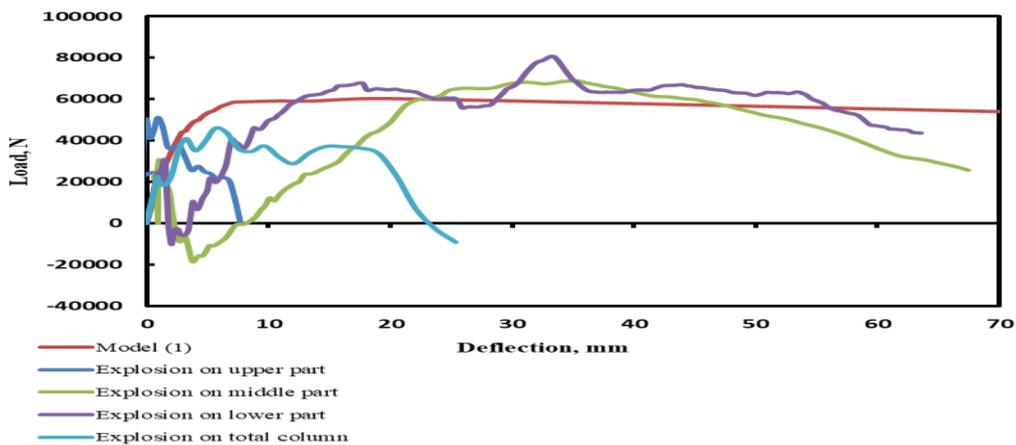
**Figure (9):** Modes of failure in both experimental and FE model (1)



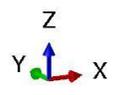
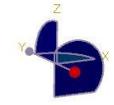
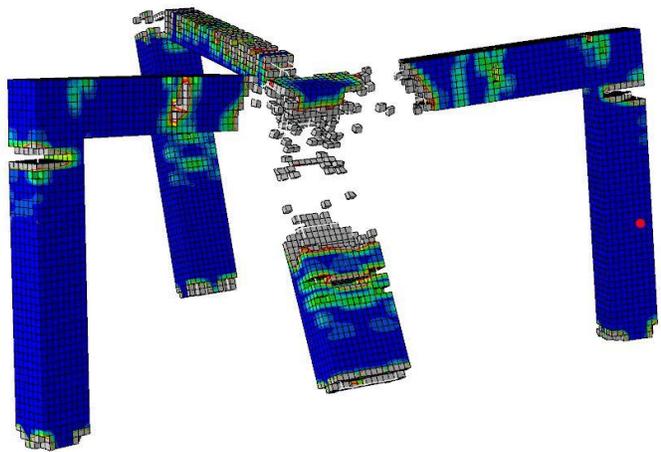
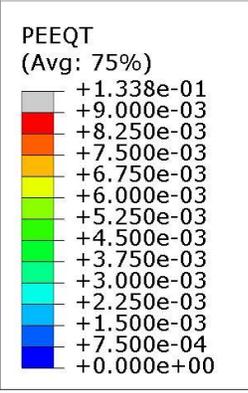
**Figure (10):** Vertical load- deflection relationships at middle column

### 5.2 Comparison between Model (1) and Model (2)

Load deflection relationships and failure patterns for the all studied cases are summed in figures (11 and 12) respectively. Besides, the participating ratios of column (B-2) in the total capacity in all cases are presented in table (3).

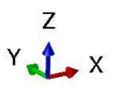
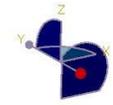
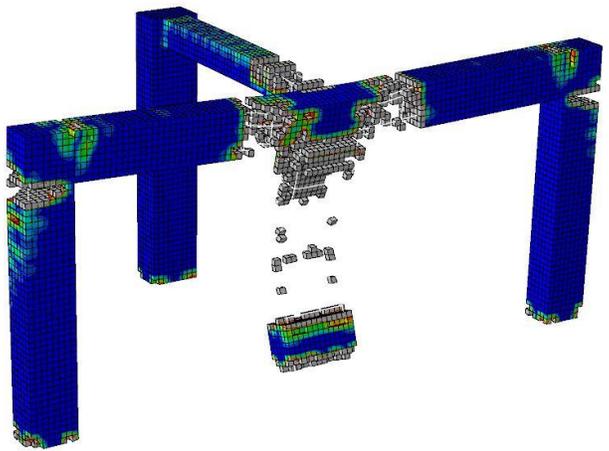
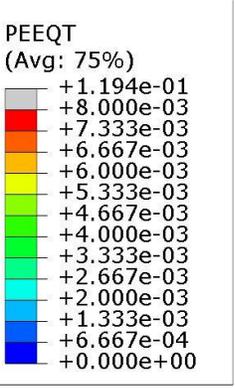


**Figure (11):** The load- deflection relationships at middle column due to Explosion load



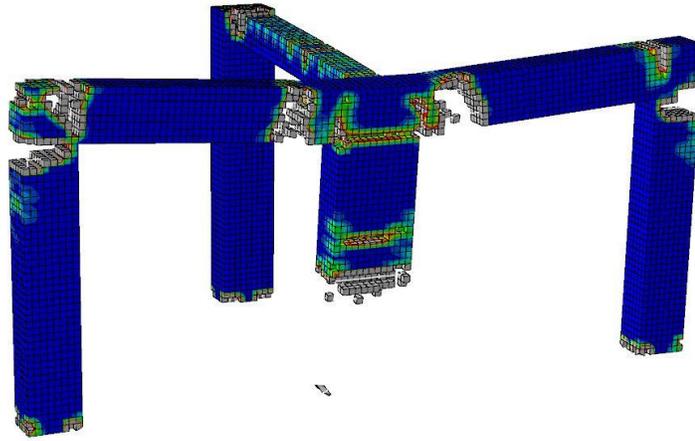
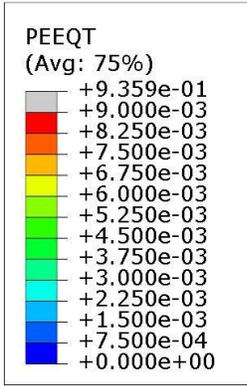
ODB: upper.odb    Abaqus/Explicit 6.14-2    Wed Feb 14 16:36:18 Egypt Standard Time 2018  
 Step: Step-1  
 Increment    96805: Step Time =    4.9417E-02  
 Primary Var: PEEQT

(a) Explosion on upper part of the column



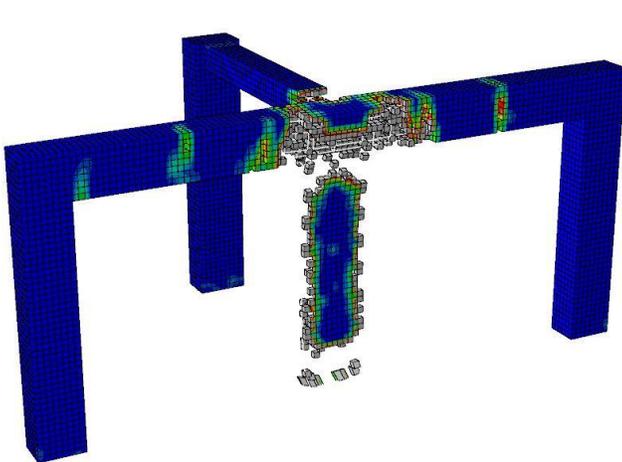
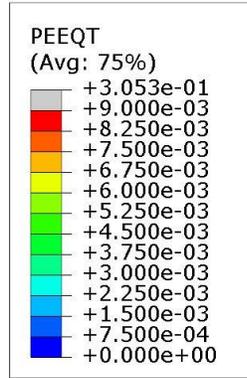
ODB: bblast1.odb    Abaqus/Explicit 6.14-2    Fri Feb 02 19:24:11 Egypt Standard Time 2018  
 Step: Step-1  
 Increment    8070: Step Time =    1.4834E-02  
 Primary Var: PEEQT

(b) Explosion on middle part of the column



Z  
Y X  
ODB: Lower.odb Abaqus/Explicit 6.14-2 Wed Feb 14 11:18:00 Egypt Standard Time 2018  
Step: Step-1  
Increment 12953: Step Time = 2.6167E-02  
Primary Var: PEEQT

(c) Explosion on middle part of the column



Z  
Y X  
ODB: Total.odb Abaqus/Explicit 6.14-2 Thu Feb 15 09:25:49 Egypt Standard Time 2018  
Step: Step-1  
Increment 2887: Step Time = 8.5837E-03  
Primary Var: PEEQT

(d) Explosion on the entire front face of the column

**Figure (11):** Failure pattern of the frame in the four cases of Model (2)

**Table (3):** The percentage of reaction at column (B-2) of total capacity of frame when explosion was applied at different position of column.

Percentage of total capacity %	Model (1)	Upper explosion	Middle explosion	Lower explosion	Explosion on total column
	6.7%	59%	20%	23%	54.5%

In general, it can be observed that when the explosion was applied to the column, the load-deflection relationships as well as the frame collapse patterns differed significantly from Model (1), where the four cases of Model (2) showed a symmetrical pattern of failure and irregular shapes of load-deflection curves in contrast to Model (1).

Moreover, the total behavior of frame was strongly dependent on the location of application of explosion load. When explosion was applied at the upper part of the column, the capacity decreased to 51 kN at 2mm indicating a sudden failure. The same case appeared when the explosion was applied to the entire column face as the capacity was 46 kN and the deflection was 6mm. Application of blast at middle part of column led to a capacity of 69 kN at 35 mm deflection while exploding the lower part of the column raised the capacity to 81 kN at 33 mm deflection.

The previous values indicate that the worst case appeared when explosion was applied at the upper part of column while the performance of the frame got better as the location of explosion moved away from the connection as the frame showed a remarkable increase in capacity.

The ratio of column B2 participation in the overall capacity reached 59% and 54.5% when explosion was applied at upper part and on the entire front face of the column respectively. This ratio decreased to 20% and 23% at middle and lower explosion. In contrast, column participation was only 6.7% in case of Model (1).

## 6 Conclusions

The main findings of the current work can be summarized as follows:

- 1- Finite element model results showed fair agreement with the tested frame regarding to mode of failure and load-deflection relationships.
- 2- Concrete at high strain rate has higher properties in both tension and compression which significantly affects the structural behavior in the numerical model.
- 3- The total behavior and failure pattern of the frame is significantly influenced by the nature and position of applications of the explosion load. So, the common methods followed to study progressive collapse by removing some elements don't represent the real behavior as they ignore the main reason of collapse.
- 4- Beside the damage that occurred in frame FR (1), there was damage that observed in the transverse beam and hence column B-2 participated in total capacity of the structure. This indicated that considering 2D structures only is not enough to express the real behavior of a structure.

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