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ANALYSIS OF WELD MOLTEN METAL KINEMATIC VISCOSITY OF TIG MILD STEEL WELD

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Abstract

Viscosity is an important property of liquid metals during welding because it controls the rate of transport of liquid metals, which may lead to weld defects such as cracks, porosity etc., which greatly affects weld quality. This study was carried out with the aim of optimizing and predicting the weld molten metal fluidity of weldment. Mild steel plate was cut into dimension 60mmx40mmx10mm with a power hacksaw, grinded and cleaned before the welding process. The experimental matrix was made of twenty (20) runs, generated by the design expert 7.01 software adopting the central composite design. The result obtained in this research study shows that a high viscosity produces weldment with better structural integrity. The model produced numerical optimal solution of current 150 amps, voltage of 20 volts and gas flow rate of 171/min will produce a welded structure having kinematic viscosity of 1.179m2/s at a desirability value of 94.6%.

Introduction

Hildebrand and Lamoreaux (1976) defined fluidity as the reciprocal of viscosity. Korolezukhejnak and Migas (2012) and Bakhtiyarov and Over felt (1999) described viscosity as a rheological property of materials which presents itself when the velocity gradient between neighbouring layers of material is deserved. These authors saw viscosity as an important rheological parameter for understanding the hydrodynamics and kinetics of reactions in metal refining, casting, metal and slag tapping or dripping. For instance, the rate of the rise of gas bubbles and non-metallic inclusions through a molten metal is primarily related to viscosity Di Sabatino et al. (2008) and Moran do et al. (2015). Also, the kinetics of reactions between metal and slag can be monitored by continuous measurements of the liquid's viscosity. Kaptay (2005) said that the viscosity of liquid metals and alloys is one of the technologically important transport properties needed to develop and optimize metallurgical technologies. Boda et al (2015) were of the opinion that viscosity of a fluid is a measure of its resistance to gradual deformation by shear stress or tensile stress. The authors said that viscosity is a property arising from collisions between neigh boring particles in a fluid that are moving at different velocities Davies (1992). When the fluid is forced by the force of the shielding gas and arc temperature, the particles which comprises the fluid generally move more quickly near the weld pool axis (center) and more slowly near the walls of the work piece (liquid-solid interface). Therefore these forces are needed to overcome the friction between particle layers and keep the fluid

moving (detaching). If any two layers of liquid move with different velocities, the top layer moves faster than the next layer due to viscous drag. It is therefore observed that the kinematic viscosity of all liquids decreases as temperature of liquids increases and vice versa.

Ritwik (2012) wrote that rheology describes the deformation and flow behaviour in all types of matter. Deformation is the process of changing the relative position of the various parts in a body. Upon deformation, spontaneous return to the undeformed shape is called elasticity, whereas an irreversible change leading to dissipation of the mechanical energy as heat is termed 'flow'. To create flow, a stress must be applied. Under an applied stress (i.e. shielding gas and arc temperature, in terms of welding) the type of deformation that occurs is known as shear. Simple shear can be visualised as a set of infinitely thin parallel plates sliding over one another as in a deck of cards. Since each plane is reluctant to move with respect to the other, there is a resistance to flow. This resistance is what is now referred to as viscosity. Due to the similarity between the frictional forces in solids, which resists the motion of one solid over another, and the resistance to flow in fluids sometimes referred to as internal friction, viscosity creates a picture in the internal friction between the different layers fluid Achebo (2012).

Materials and Methods

Materials

100 pieces of mild steel coupons measuring 80 x 40 x10 was used for the experiments, the experiment was performed 20 times using 5 specimens for each run. The key parameters considered in this work are welding current, welding speed, gas flow rate, and welding voltage. The range of the process parameters obtained from literature which is shown in the table 1. The tungsten inert gas welding equipment was used to weld the plates after the edges have been bevelled and machined. Figure 1 shows the TIG welding setup. The welding process uses a shielding gas to protect the weld specimen from atmospheric interaction, 100% pure Argon gas was used in this research study. Figure 2 shows the shielding gas cylinder and regulator. Figure 3 shows the weld sample



Figure 1: TIG equipment



Figure 2: shielding gas cylinder and regulator



Factors	Unit	Symbol	Low (-1)	High (+1)
Welding Current	Ampere	Ι	130	170
Welding Voltage	Volts	V	20	24
Gas Flow Rate	Lit/min	GFR	13	17



Figure 3 weld samples

Method of Data Collection

The central composite design matrix was developed using the design expert software, producing 20 experimental runs. The input parameters and output parameters make up the experimental matrix and the responses recorded from the weld samples was used as the data. The data matrix is determined by the number of input parameters which is expressed in the equation 2n + 2n + k, where k is number of center points, 2n is the number of axial points and 2n is the number of factorial points.

The matrix can be expressed in actual values which fall within the range stated, is presented in figure 4

File Edit View Display	Opti	ons E	Design	Tools Help			
		23	Q :				
Design (Actual)		Std	Run	Туре	Factor 1 A:Current Ampere	Factor 2 B:Voltage Volts	Factor 3 C:Gas Flow Ra L/min
Graph Columna		15	1	Center	165.00	22.00	15.50
		17	2	Center	165.00	22.00	15.50
Malysis		16	3	Center	165.00	22.00	15.50
- J Surface Tension (A		19	4	Center	165.00	22.00	15.50
🗜 Fluidity (Analyzed)		20	5	Center	165.00	22.00	15.50
Kinematic Viscosity		18	6	Center	165.00	22.00	15.50
I 🔄 Optimization		10	7	Axial	190.23	22.00	15.50
···) Numerical		11	8	Axial	165.00	18.64	15.50
Graphical		12	9	Axial	165.00	25.36	15.50
in <u>ki</u> Point Prediction		9	10	Axial	139.77	22.00	15.50
		14	11	Axial	165.00	22.00	18.02
		13	12	Axial	165.00	22.00	12.98
		4	13	Fact	180.00	24.00	14.00
		1	14	Fact	150.00	20.00	14.00
		2	15	Fact	180.00	20.00	14.00
		5	16	Fact	150.00	20.00	17.00
		3	17	Fact	150.00	24.00	14.00
		6	18	Fact	180.00	20.00	17.00
		7	19	Fact	150.00	24.00	17.00
		8	20	Fact	180.00	24.00	17.00

Figure 4: Central Composite Design Matrix (CCD) in actual values

Model Validation for ANOVA

i) Coefficient of determination R^2

The coefficient of determination R^2 was used to validate the developed model equation 1 shows the expression for the diagnostic tool. The model targetispredicted using the R^2 .

$$R^{2} = \frac{\sum_{i=1}^{n} (y_{i} - \hat{y}_{i})^{2}}{\sum_{i=1}^{n} (y_{i} - \hat{y}_{i})^{2}}$$
(1)

The experimental observation is represented with . is the fitted observation.

is the average observation

 $R^2 \le 1$ (R^2 is less than or equal to one in most cases)

ii) The adjusted coefficient determination is determined and used to validate the developed model.

It is expressed in equation 2.

$$AdjR^{2} = \frac{\sum_{i=1}^{n} \frac{y_{i} - y_{i}}{n-k}}{\sum_{i=1}^{n} \frac{y_{i} - y_{i}}{n-1}}$$
(2)

When n is the input process parameters, K is the no of responses and the observation for the experiment is represented with yi and y is fitted observation with y as the average observation. R^2 value is always below 1 (Ibrahim IBN, 2009).

RESULTS AND DISCUSSION

The design matrix showing the real value of three input variables namely; current (Amp), voltage (volts) and gas flow rate (L/min) and three responses namely; (surface tension, fluidity and kinematic viscosity) is presented in Figure 5

	8	? ×	ç t							
Design (Actual)		Std	Run	Туре	Factor 1 A:Current Ampere	Factor 2 B:Voltage Volts	Factor 3 C:Gas Flow Ra L/min	Response 1 Surface Tensic N/m	Response 2 Fluidity ms/kg	Response 3 Kinematic Viscosity (m^2/s)*10^-6
Graph Columns		15	1	Center	165.00	22.00	15.50	1.1095	123.333	1.209
• Evaluation		17	2	Center	165.00	22.00	15.50	1.3093	132.345	1.112
III Analysis		16	3	Center	165.00	22.00	15.50	1.3087	133.421	1.108
🕌 Surface Tension (A		19	4	Center	165.00	22.00	15.50	1.3092	134.021	1.114
📔 Fluidity (Analyzed)		20	5	Center	165.00	22.00	15.50	1.3095	133.245	1.106
🕌 Kinematic Viscosity		18	6	Center	165.00	22.00	15.50	1.2097	132.434	1.108
🔄 Optimization		10	7	Axial	190.23	22.00	15.50	1.2175	135.564	1.0544
Mumerical		11	8	Axial	165.00	18.64	15.50	1.2032	136.986	1.0578
Graphical		12	9	Axial	165.00	25.36	15.50	1.0875	144.928	1.01
Point Prediction		9	10	Axial	139.77	22.00	15.50	1.2147	154.563	1.1456
		14	11	Axial	165.00	22.00	18.02	1.4637	126.582	1.2638
		13	12	Axial	165.00	22.00	12.98	1.3988	140.845	1.2457
		4	13	Fact	180.00	24.00	14.00	1.0004	144.928	1.0049
		1	14	Fact	150.00	20.00	14.00	1.5115	143.333	1.0041
		2	15	Fact	180.00	20.00	14.00	1.5448	118.279	1.4371
		5	16	Fact	150.00	20.00	17.00	1.0149	141.579	1.2234
		3	17	Fact	150.00	24.00	14.00	1.0689	162.996	1.0068
		6	18	Fact	180.00	20.00	17.00	1.0171	145.475	1.0008
		7	19	Fact	150.00	24.00	17.00	1.4845	117.059	1.508
		8	20	Fact	180.00	24.00	17.00	1.4904	124.928	1.0009

Figure 5: Design matrix showing the real values and the experimental values

The model summary which shows the factors and their lowest and highest values including the mean and standard deviation is presented as shown in Table 6; Result of Table 6 revealed that the model is of the quadratic type which requires the polynomial analysis order as depicted by a typical response surface design. The minimum value of kinematic viscosity was observed to be $1.001 \times 10^{-6} \text{m}^2/\text{s}$, the maximum value was observed to be $1.508 \times 10^{-6} \text{m}^2/\text{s}$, with a mean value of $1.136 \times 10^{-6} \text{and}$ standard deviation of 0.140×10^{-6} .

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Notes for FLUIDITY												
🏢 Design (Coded)	Design Sun	nmary										
- 🖻 Summary		_										
🔄 Graph Columns	Study Type	Response Sur	face	Runs	20							
🕙 Evaluation	Initial Desig	n Central Compo	site	Blocks	No Blocks							
- 📕 Analysis	Design May	del Quadratia										
- 📗 Surface Tension (A	Design Mod	Jer Quadratic										
- 🗼 Fluidity (Analyzed)												
- 🗼 Kinematic Viscosity	Factor	Name	Units	Туре	Low Actual	High Actual	Low Coded	High Coded	Mean	Std. Dev.		
🛄 🚺 Optimization	A	Current	Ampere	Numeric	150.00	180.00	-1.000	1.000	165.000	12.395		
-Mumerical	В	Voltage	Volts	Numeric	20.00	24.00	-1.000	1.000	22.000	1.653		
🌇 Graphical	c	Gas Flow Rate	L/min	Numeric	14.00	17.00	-1.000	1.000	15.500	1.240		
È Point Prediction												
	Response	Name	Units	Obs	Analysis	Minimum	Maximum	Mean	Std. Dev.	Ratio	Trans	Model
	Y1	Surface Tensic	or N/m	20	Polynomial	1.000	1.545	1.264	0.174	1.544	None	Quadratic
	Y2	Fluidity	ms/kg	20	Polynomial	117.059	162.996	136.342	11.222	1.392	None	Quadratic
	Y3	Kinematic Visc	:o: (m^2/s)*10^-6	20	Polynomial	1.001	1.508	1.136	0.140	1.507	None	Quadratic

Figure 6: RSM design summary

To validate the suitability of the quadratic model in analyzing the experimental data, the sequential model sum of squares were calculated for kinematic viscosity as presented in figure 7

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Summary										
Graph Columns	Response 3	3	Kinematic Viso	Transform:	None					
🕙 Evaluation	*** WARNING: T	he Cubic Mod	el is Aliased! **	*						
Analysis	_									
- 🚺 Surface Tension (A	Sequential Mod	Sequential Model Sum of Squares [Type I]								
- Fluidity (Analyzed)		Sum of		Mean	F	p-value				
Kinematic Viscos	Source	Squaree	df	Square	Value	Prob > F				
···· 🚰 Optimization	Source	Squares	ui 4	Square of 04	value	FIODET				
	Mean vs Total	25.61	1	25.61						
💹 Graphical	Linear vs Mean	0.026	3	8.579E-003	0.38	0.7713				
Point Prediction	2Fl vs Linear	0.30	3	0.099	18.96	< 0.0001				
	Quadratic vs 2FI	0.052	<u>3</u>	0.017	<u>11.25</u>	0.0015	Suggested			
	Cubic vs Quadra	6.135E-003	4	1.534E-003	0.98	0.4826	Aliased			
	Residual	9.369E-003	6	1.562E-003						
	Total	26.20	20	1.31						

Figure 7: Sequential model sum of square for kinematic viscosity

The sequential model sum of squares table shows the accumulating improvement in the model fit as terms are added. Based on the calculated sequential model sum of square, the highest order polynomial where the additional terms are significant and the model is not aliased was selected as the best fit. From the results of figure 7 it was observed that the cubic polynomial was aliased hence cannot be employed to fit the final model. In addition, the quadratic and 2FI model were suggesed as the best fit thus justifying the use of quadratic polynomial in this analysis

To test how well the quadratic model can explain the underlying variation associated with the experimental data, the lack of fit test was estimated for kinematic viscosity. Model with significant lack of fit cannot be employed for prediction. Results of the computed lack of fit is presented in Figure 8.

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Notes for FLUIDITY	y ^λ Transform	Fit Summary	f(x) Model		Diagno	ostics Mode	IGraphs
🏥 Summary							
🔄 Graph Columns							
🖄 Evaluation							
- Analysis	Lack of Fit Tes	sts					
Surface Tension (A		Sum of		Mean	F	p-value	
Kinomatia Viscos	Source	Squares	df	Square	Value	Prob > F	
Optimization	Linear	0.36	11	0.032	19.58	0.0021	
- Mumerical	2FI	0.060	8	7.445E-003	4.50	0.0572	
🌇 Graphical	Quadratic	7.228E-003	<u>5</u>	1.446E-003	<u>0.87</u>	0.5573	Suggested
Point Prediction	Cubic	1.092E-003	1	1.092E-003	0.66	0.4535	Aliased
	Pure Error	8.277E-003	5	1.655E-003			
	"Lack of Fit Te:	sts": Want the se	lected model to h	nave insignificant l	ack-of-fit.		
	Figure 8.	Lack of fi	t test for l	vinematic v	viscositv		

The model summary statistics computed for kinematic viscosity is presented in figure9

Model Summary Statistics												
	Std.		Adjusted	Predicted								
Source	Dev.	R-Squared	R-Squared	R-Squared	PRESS							
Linear	0.15	0.0659	-0.1092	-0.7252	0.67							
2FI	0.072	0.8263	0.7461	0.6168	0.15							
Quadratic	0.039	0.9603	0.9246	0.8176	<u>0.071</u>	Suggested						
Cubic	0.040	0.9760	0.9240	0.3528	0.25	Aliased						
 "Model Summary Sta and the "Predicted R	a <i>tistics"</i> : Foc -Squared".	us on the model	maximizing the "/	Adjusted R-Square	ed"							

Figure 9: Model summary statistics for kinemstic viscosity

Analysis of the model standard error was employed to assess the suitability of response surface methodology using the quadratic model to minimize the surface tension, maximize the fluidity and maximize the kinematic viscosity. The computed standard errors for the selected responses are presented in figure 10.

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- 📑 Design (Coded)		() Woder	III Results	Graphs							
- 📑 Summary											
- 🔄 Graph Columns		Power at 5 % alpha level for effect of									
Evaluation		Term	StdErr**	VIF	Ri-Squared	0.5 Std. Dev.	1 Std. Dev.	2 Std. Dev.			
- Analysis		А	0.27	1.00	0.0000	13.3 %	38.6 %	91.4 %			
Surface Tension (A		в	0.27	1.00	0.0000	13.3 %	38.6 %	91.4 %			
Fluidity (Analyzed)		С	0.27	1.00	0.0000	13.3 %	38.6 %	91.4 %			
Contimization		AB	0.35	1.00	0.0000	9.8 %	24.9 %	72.2 %			
Numerical		AC	0.35	1.00	0.0000	9.8 %	24.9 %	72.2 %			
Graphical		BC	0.35	1.00	0.0000	9.8 %	24.9 %	72.2 %			
Point Prediction		A ²	0.26	1.02	0.0179	40.4 %	92.7 %	99.9 %			
		B ²	0.26	1.02	0.0179	40.4 %	92.7 %	99.9 %			
		C ²	0.26	1.02	0.0179	40.4 %	92.7 %	99.9 %			
		**Basis Std. D	ev. = 1.0								

Figure 10: Result of computed standard errors

From the results of figure 10, it was observed that the model possess a low standard error ranging from 0.27 for the individual terms, 0.35 for the combine effects and 0.26 for the quadratic terms. Standard errors should be similar within type of coefficient; smaller is better. The error values were also observed to be less than the model basic standard deviation of 1.0 which suggests that response surface methodology was ideal for the optimization process. Variance inflation factor (VIF) of approximately 1.0 as observed in Table 10 was good since ideal VIF is 1.0. VIF's

above 10 are cause for alarm, indicating coefficients are poorly estimated due to multicollinearity. In addition, the Ri-squared value was observed to be between 0.0000 to 0.0179 which is good. High Ri-squared (above 1.0) means that design terms are correlated with each other, possibly leading to poor models. The correlation matrix of regression coefficient is presented in figure 11

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Notes for FLUIDITY			B. Desults	-	1					
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Graph Columns		Correlation I	Matrix of Regres	sion Coefficie	nts					
Evaluation		1	Intercept	А	в	с	AB	AC	BC	
🔟 Analysis		Intercept	1.000							
🗼 Surface Tension (A		Δ.	-0.000	1 000						
- J Fluidity (Analyzed)			0.000	0.000	1 000					
Kinematic Viscosity			-0.000	-0.000	1.000	4 000				
🦾 🌄 Optimization		C	-0.000	-0.000	-0.000	1.000				
🔀 Numerical		AB	-0.000	-0.000	-0.000	-0.000	1.000			
🎦 Graphical		AC	-0.000	-0.000	-0.000	-0.000	-0.000	1.000		
🖹 Point Prediction		BC	-0.000	-0.000	-0.000	-0.000	-0.000	-0.000	1.000	
		A ²	-0.529	-0.000	-0.000	-0.000	-0.000	-0.000	-0.000	
		B ²	-0.529	-0.000	-0.000	-0.000	-0.000	-0.000	-0.000	
		C ²	-0.529	-0.000	-0.000	-0.000	-0.000	-0.000	-0.000	
		1								

Figure 11: Correlation matrix of regression coefficients

Lower values of the off diagonal matrix as observed in Table 11 indicates a well fitted model that is strong enough to navigate the design space and adequately optimize the selected response variables. From the results of figure 11, it was observed that the off diagonal matrix had coefficients that were approximately 0.00 which is an indication that the quadratic model was the ideal one for this analysis since off diagonal matrix greater than 0.00 is cause for alarm indicating a model having coefficients that are poorly correlated.

To understand the influence of the individual design points on the model's predicted value, the model leverages were computed as presented in figure 12

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Notes for FLUIDITY	f(x) Model	Benutte		1	
III Design (Coded)					
🛄 Summary					
Graph Columns	Std	Leverage	Point Type		
🕅 Evaluation	1	0.6698	Fact		
Analysis	2	0.6698	Fact		
Surface Tension (A	3	0.6698	Fact		
Kinematic Viscosity	4	0.6698	Fact		
	5	0.6698	Fact		
Numerical	6	0.6698	Fact		
🕅 Graphical	7	0.6698	Fact		
Ŷ: Point Prediction	8	0.6698	Fact		
	9	0.6073	Axial		
	10	0.6073	Axial		
	11	0.6073	Axial		
	12	0.6073	Axial		
	13	0.6073	Axial		
	14	0.6073	Axial		
	15	0.1663	Center		
	16	0.1663	Center		
	17	0.1663	Center		
	18	0.1663	Center		
	19	0.1663	Center		
	20	0.1663	Center		
	Average =	0.5000			



Leverage of a point varies from 0 to 1 and indicates how much an individual design point influences the model's predicted values. A leverage of 1 means the predicted value at that particular case will exactly equal the observed value of the experiment, i.e., the residual will be 0. The sum of leverage values across all cases equals the number of coefficients (including the constant) fit by the model. The maximum leverage an experiment can have is 1/k, where k is the number of times the experiment was replicated.

In assessing the strength of the quadratic model towards maximizing the kinematic viscosity, one way analysis of variance (ANOVA) was done and result is presented in figure 13

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Graph Columns					I		
- Staphicolamic	Use your mouse to	a ngint click on individ	iual cells for defin	iuons.			
Analysis	Response	3	Kinematic Visc	osity			
Surface Tension (A	ANOVA for F	Response Surface	Quadratic Mode	el			
- Fluidity (Analyzed)	Analysis of varia	ince table [Partial	sum of squares	- Type III]			
Kinematic Viscos		Sum of		Mean	F	p-value	
Optimization	Source	Squares	df	Square	Value	Prob > F	
- Mumerical	Model	0.37	9	0.042	26.87	< 0.0001	significant
🌄 Graphical	A-Current	0.015	1	0.015	9.65	0.0111	
Point Prediction	B-Voltage	3.713E-003	1	3.713E-003	2.39	0.1528	
	C-Gas Flow Rate	7.066E-003	1	7.066E-003	4.56	0.0585	
	AB	0.065	1	0.065	41.73	< 0.0001	
	AC	0.17	1	0.17	108.64	< 0.0001	
	BC	0.064	1	0.064	41.12	< 0.0001	
	A ²	4.123E-004	1	4.123E-004	0.27	0.6173	
	B ²	0.012	1	0.012	7.67	0.0198	
		0.035	1	0.035	22.65	0.0008	
	Residual	0.016	10	1.550E-003			
	Lack of	Fit 7 228E-003		1 446E-003	0.87	0 5573	not significant
	- Dure E	mor 8 277E 003	5	1.6555 003	0.07	0.0070	not arginitedit
		0.2772-003	10	1.000E-000			
	Corrotal	0.39	19				

Figure 13: ANOVA table for validating the model significance towards maximizing the kinematic viscosity

Analysis of variance (ANOVA) was needed to check whether or not the model is significant and also to evaluate the significant contributions of each individual variable, the combined and quadratic effects towards each response.

From the result of figure 13, the Model F-value of 26.87 implies the model is significant. There is only a 0.01% chance that a "Model F-Value" this large could occur due to noise. Values of "Prob > F" less than 0.0500 indicate model terms are significant. In this case A, AB, AC, BC, B2, C2 are significant model terms. Values greater than 0.1000 indicate the model terms are not significant. The "Lack of Fit F-value" of 0.87 implies the Lack of Fit is not significant relative to the pure error. There is a 55.73% chance that a "Lack of Fit F-value" this large could occur due to noise. Non-significant lack of fit is good as it indicates a model that is significant.

To validate the adequacy of the quadratic model based on its ability to maximize the kinematic viscosity, the goodness of fit statistics presented in figure 14 were employed;

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🏥 Summary								
- 🔄 Graph Columns		Std. Dev.	(0.039	R-Squared	0.9603		
🕙 Evaluation		Mean		1.14	Adj R-Squared	0.9246		
- Analysis		C.V. %		3.47	Pred R-Squared	0.8176		
- J Surface Tension (A		PRESS	(0.071	Adeq Precision	19.260		
Fluidity (Analyzed)		1						
	_							
. Dotimization		The "Pred R-So	quared" of 0.8176 i	is in reasonable	agreement with the "A	dj R-Squared" of (0.9246.	

Figure 14: GOF statistics for validating model significance towards maximizing the kinematic viscosity

From the result of figure 14 it was observed that the "Predicted R-Squared" value of 0.8176 is in reasonable agreement with the "Adj R-Squared" value of 0.9246. Adequate precision measures the signal to noise ratio. A ratio greater than 4 is desirable. The computed ratio of 19.260as observed in figure 14indicates an adequate signal. This model can be used to navigate the design space and maximize the kinematic viscosity

To obtain the optimal solution, we first consider the coefficient statistics and the corresponding standard errors. The computed standard error measures the difference between the experimental terms and the corresponding predicted terms. Coefficient statistics for kinematic viscosity is presented in figure 15

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	a ? 😵											
Notes for FLUIDITY	y ^λ Transform	Fit Summary f(x) M	odel 🕂	ANOVA	🛻 Diagnostics	Model Graphs						
Summary		1 1		ī		1	1					
Graph Columns		Coefficient		Standard	95% CI	95% CI						
	Eactor	Estimate	df	Error	Low	High	VIE					
		Latinate	4	0.040	1.00	1.40						
Surface Tension (A)		1.13	1	0.016	1.09	1.16						
	A-Current	-0.033	1	0.011	-0.057	-9.355E-003	1.00					
Kinematic Viscos	B-Voltage	-0.016	1	0.011	-0.040	7.252E-003	1.00					
	C-Gas Flow Rate	0.023	1	0.011	-9.946E-004	0.046	1.00					
Numerical	AB	-0.090	1	0.014	-0.12	-0.059	1.00					
Graphical	AC	-0.15	1	0.014	-0.18	-0.11	1.00					
👬 Point Prediction	BC	0.089	1	0.014	0.058	0.12	1.00					
	A ²	-5.348E-003	1	0.010	-0.028	0.018	1.02					
	B ²	-0.029	1	0.010	-0.052	-5.607E-003	1.02					
	C ²	0.049	1	0.010	0.026	0.072	1.02					

Figure 15: Coefficient estimates statistics towards maximizing kinematic viscosity

Variance inflation factor (VIF) value of 1.00 for the individual and combine terms, 1.02 for the quadratic terms as observed in Table 15 indicate a significant model in which the variables are highly correlated with the responses.

The optimal equation which shows the individual effects and combines interactions of the selected input variables (current, voltage and gas flow rate) against the mesured responses (kinematic viscosity) is presented based on the coded variables in figure 16.

-	
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Notes for FLUIDITY	
🎹 Design (Coded)	
🏥 Summary	
📴 Graph Columns	Final Equation in Terms of Coded Factors:
🕙 Evaluation	
🖬 Analysis	Kinematic Viscosity =
🕌 Surface Tension (A	-113
📕 Fluidity (Analyzed)	
🚺 Kinematic Viscos	
🔛 Optimization	
🔀 Numerical	+0.023 * C
💹 Graphical	-0.090 * A * B
Point Prediction	-0.15 * A * C
	+0.089 * B * C
	-0.029 *B ²
	+0.049 * C ²
	+0.049 * C ²

Figure 16: Optimal equation in terms of coded factors for maximizing kinematic viscosity

The optimal equation which shows the individual effects and combine interactions of the selected input variables (current, voltage and gas flow rate) against (kinematic viscosity is presented in actual factors in figure17



Figure 17: Optimal equation in terms of actual factors for maximizing kinematic viscosity The diagnostics case statistics which shows the observed values of each response variable (kinematic viscosity) against the predicted values is presented in figure 18. The diagnostic case statistics actually give insight into the model strength and the adequacy of the optimal second order polynomial equation.

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Notes for FLUIDITY		A Transform				Disgration	- Model Graph	al			
III Design (Coded)	<u>y</u>	manaronn	The Stammon y		0140 10	· · ·	Moder or april	a.			
🔢 Summary											
Graph Columns		Response	3	Kinematic Viscosity	Transform:	None					
L. S Evaluation											
Analysis		Diagn	ostics Case Sta	tistics							
Surface Tension (A							Internally	Externally	Influence on		
Finance (Analyzed)		Standard	Actual	Predicted			Studentized	Studentized	Fitted Value	Cook's	Run
		Order	Value	Value	Residual	Leverage	Residual	Residual	DFFITS	Distance	Order
Numerical		1	1.00	1.02	-0.018	0.670	-0.789	-0.773	-1.101	0.126	14
Graphical		2	1.44	1.43	0.011	0.670	0.499	0.479	0.682	0.050	15
Point Prediction		3	1.01	0.99	0.017	0.670	0.730	0.712	1.014	0.108	17
		4	1.00	1.03	-0.030	0.670	-1.305	-1.360	-1.936	0.346	13
		5	1.22	1.18	0.044	0.670	1.958	2.365	* 3.37	0.777	16
		6	1.00	1.00	-1.756E-003	0.670	-0.078	-0.074	-0.105	0.001	18
Diagnostics Tool		7	1.51	1.50	3.481E-003	0.670	0.154	0.146	0.208	0.005	19
Diagnostics Influence		8	1.00	0.97	0.033	0.670	1.442	1.537	* 2.19	0.422	20
		9	1.15	1.17	-0.021	0.607	-0.831	-0.817	-1.016	0.107	10
		10	1.05	1.05	-3.821E-004	0.607	-0.015	-0.015	-0.018	0.000	7
Ext. Student ei		11	1.06	1.07	-0.014	0.607	-0.578	-0.558	-0.694	0.052	8
Leverage		12	1.01	1.02	-6.610E-003	0.607	-0.268	-0.255	-0.317	0.011	9
DEPETAS		13	1.25	1.23	0.019	0.607	0.760	0.743	0.924	0.089	12
Cook's D		14	1.26	1.30	-0.040	0.607	-1.607	-1.770	* -2.20	0.399	11
Report		15	1.21	1.13	0.083	0.166	2.321	3.241	1.448	0.107	1
		16	1.11	1.13	-0.018	0.166	-0.489	-0.469	-0.210	0.005	3
		17	1.11	1.13	-0.014	0.166	-0.377	-0.361	-0.161	0.003	2
		18	1.11	1.13	-0.018	0.166	-0.489	-0.469	-0.210	0.005	6
Clear Points		19	1.11	1.13	-0.012	0.166	-0.322	-0.307	-0.137	0.002	4
		20	1.11	1.13	-0.020	0.166	-0.544	-0.524	-0.234	0.006	5

Figure 18: Diagnostics case statistics report of observed and predicted kinematic viscosity

Lower residual values resulting to higher leverages as observed in figure 18 are indicators of a well fitted model.

To assess the accuracy of prediction and established the suitability of response surface methodology using the quadratic model, a reliability plot of the observed and predicted values of kinematic viscosity was obtained as presented in Figures 19



Figure 19: Reliability plot of observed versus predicted kinematic viscosity Figure 20: Normal probability plot of Student zed residuals for kinematic viscosity

The high coefficient of determination ($r_2 = 0.9288$, 0, 9438 and 0.9603) as observed in Figure 19 were used to established the suitability of response surface methodology in maximizing the kinematic viscosity

To accept any model, its satisfactoriness must first be checked by an appropriate statistical analysis output. To diagnose the statistical properties of the kinematic viscosity model, the normal probability plot of residual presented in Figure 20

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The normal probability plot of student zed residuals was employed to assess the normality of the calculated residuals. The normal probability plot of residuals which is the number of standard deviation of actual values based on the predicted values was employed to ascertain if the residuals (observed – predicted) follows a normal distribution. It is the most significant assumption for checking the sufficiency of a statistical model. Results of Figures 20 revealed that the computed residuals are approximately normally distributed an indication that the model developed is satisfactory and the data employed are devoid of possible outliers.

To determine the presence of a possible outlier, the cook's distance plot was generated for the kinematic viscosity. The cook's distance is a measure of how much the regression would change if the outlier is omitted from the analysis. A point that has a very high distance value relative to the other points may be an outlier and should be investigated. The generated cook's distance is presented in Figures 21



Figure 21: Generated cook's distance for kinematic viscosity Figure 22: Effect of current and voltage on kinematic viscosity

To study the effects of combine input variables on kinematic viscosity 3D surface plots is presented in Figure 22. The 3D surface plot as observed in Figure 22 shows the relationship between the input variables (current, voltage and gas flow rate) and the response variables (surface tension, fluidity and kinematic viscosity). It is a 3 dimensional surface plot which was employed to give a clearer concept of the response surface. Although not as useful as the contour plot for establishing responses values and coordinates, this view may provide a clearer view of the surface. As the colour of the curved surface gets darker, the surface tension decreases proportionately while the fluidity and kinematic viscosity increases. The presence of a coloured hole at the middle of the upper surface gave a clue that more points lightly shaded for easier identification fell below the surface.

Finally, numerical optimization was performed to ascertain the desirability of the overall model. In the numerical optimization phase, we ask design expert to; determine the optimum current (Amp), voltage (volts) and gas flow rate (L/min) that will maximize kinematic viscosity, The interphase of the numerical optimization showing the objective function is presented in Figure 23

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Notes for FLUIDITY Design (Actual) Graph Columns Analysis Analysis Surface Tension (A L Fluidity (Analyzed) Kinematic Viscosity Dytimization Numerical	Criteria Solutions Graphs Current Kinematic Viscosity Gas Flow Rate Goal Surface Tension Goal Fluidity Lower Upper Limits: Limits: 1.508 Weights: 0.1 Importance: +++++
🕍 Graphical	1.0008 1.508 Kinematic Viscosity

Figure 23: Interphase of numerical optimization model for maximizing kinematic viscosity

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Notes for FLUIDITY	Criteria	Solutions	Graphs								
- 🎫 Summary	Solutions 1 2	3 4	5 6 7	8 9	10 11 1	2 13 14	15 16				
- Graph Columns											
- Analysis	Constraints										
Surface Tension (A			Lower	Upper	Lower	Upper					
🚺 Fluidity (Analyzed)	Name	Goal	Limit	Limit	Weight	Weight	Importance				
Kinematic Viscosity	Current	is in range	150	180	1	1	3				
🦾 🌄 Optimization	Voltage	is in range	20	24	1	1	3				
- 🕅 Numerical	Gas Flow Rate	is in range	14	17	1	1	3				
- 💹 Graphical	Surface Tensior	minimize	1.0004	1.5448	1	0.1	5				
	Fluidity	maximize	117.059	162.996	0.1	1	5				
	Kinematic Visco	maximize	1.0008	1.508	0.1	1	5				

The constraint set for the numerical optimization algorithm is presented in figure 24.

Figure 24: Constraints for numerical optimization of selected responses

The numerical optimization generated about sixteen (16) optimal solutions which are presented in figure 25

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Solutions 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 Craph Colums Solutions Image: Solutions S	m Design (Actual)		Solutions	Graphs								
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Solutions Solutions Analysis Number Current Voltage Gas Flow Rate Surface Tensic Fluidity Kinematic Visc Desirability Solutions 1 150.00 20.00 17.00 1.02253 143.331 1.17915 0.946 Selected Solutions 2 150.00 20.07 17.00 1.02253 143.121 1.1868 0.946 Mumerical 3 150.00 20.07 17.00 1.03643 142.731 1.8688 0.946 Solutions 3 150.00 20.01 17.00 1.04144 142.461 1.19036 0.946 Solutions Tool 6 150.00 20.02 16.99 1.02972 143.148 1.8007 0.946 7 150.67 20.12 17.00 1.04597 142.003 1.18845 0.945 8 150.00 20.05 16.93 1.03875 142.913 1.17657 0.945 9 150.00 24.00 15.35 1.17862	🔄 Graph Columns											
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Optimization 3 150.00 20.07 17.00 1.03643 142.731 1.18688 0.946 Numerical 4 150.00 20.01 17.00 1.04144 142.461 1.19036 0.946 Graphical 5 150.19 20.01 17.00 1.02171 143.195 1.17871 0.946 7 150.67 20.12 17.00 1.02571 143.195 1.17871 0.946 8 150.00 20.02 16.99 1.02972 143.148 1.18007 0.946 7 150.67 20.12 17.00 1.04597 142.003 1.18845 0.945 8 150.00 20.05 16.93 1.03875 142.913 1.17657 0.945 9 150.00 24.00 15.33 1.17862 144.999 1.17343 0.936 11 150.00 24.00 15.35 1.17808 144.867 1.1708 0.936 12 150.27 24.00 15.35	Kinematic Viscosity	2	150.00	20.03	17.00	1.02925	143.121	1.18186	0.946			
Image: Comparison 4 150.00 20.10 17.00 1.04144 142.461 1.19036 0.946 Graphical 5 150.19 20.01 17.00 1.02671 143.195 1.17871 0.946 Image: Comparison 6 150.00 20.02 16.99 1.02671 143.195 1.17871 0.946 7 150.67 20.12 17.00 1.04597 142.003 1.18845 0.945 8 150.00 20.00 16.94 1.03001 143.332 1.17254 0.945 9 150.00 20.05 16.93 1.03875 142.913 1.17657 0.945 10 150.00 24.00 15.35 1.17862 144.999 1.17343 0.936 11 150.00 24.00 15.35 1.17808 144.667 1.1708 0.936 12 150.27 24.00 15.35 1.17808 144.867 1.14337 0.924 13 150.00 21.37 16.23 1.21852 136.854 1.20722 0.928 14 180	I 🛃 Optimization	3	150.00	20.07	17.00	1.03643	142.731	1.18688	0.946			
Graphical 5 150.19 20.01 17.00 1.02671 143.195 1.17871 0.946 Model 6 150.00 20.02 16.99 1.02972 143.148 1.18007 0.946 7 150.67 20.12 17.00 1.04597 142.003 1.18845 0.945 8 150.00 20.00 16.94 1.03001 143.332 1.17254 0.945 9 150.00 20.05 16.93 1.03875 142.913 1.17657 0.945 10 150.00 24.00 15.35 1.17862 144.999 1.17343 0.936 11 150.00 24.00 15.35 1.17608 144.867 1.1708 0.936 12 150.27 24.00 15.35 1.17608 144.867 1.1708 0.936 13 150.00 21.37 16.23 1.21852 136.854 1.20722 0.928 14 180.00 23.09 14.00 1.13934 13	- Mumerical	4	150.00	20.10	17.00	1.04144	142.461	1.19036	0.946			
Image: Solutions Tool 6 150.00 20.02 16.99 1.02972 143.148 1.18007 0.946 Solutions Tool 8 150.00 20.00 16.94 1.03001 143.332 1.17254 0.945 9 150.00 20.05 16.93 1.03001 143.332 1.17254 0.945 10 150.00 24.00 15.35 1.17657 142.913 1.17657 0.945 11 150.00 24.00 15.35 1.17548 145.924 1.16995 0.936 12 150.27 24.00 15.35 1.17608 144.867 1.1708 0.936 13 150.00 21.37 16.23 1.21852 136.854 1.20722 0.928 14 180.00 23.09 14.00 1.13934 1.14337 0.924 15 180.00 23.28 14.00 1.10988 139.042 1.12211 0.923 16 180.00 22.57 14.00 1.21949 133	🔯 Graphical	5	150.19	20.01	17.00	1.02671	143.195	1.17871	0.946			
Solutions Tool 7 150.67 20.12 17.00 1.04597 142.003 1.18845 0.945 8 150.00 20.00 16.94 1.03001 143.332 1.17254 0.945 9 150.00 20.05 16.93 1.03875 142.913 1.17657 0.945 10 150.00 24.00 15.35 1.17662 144.999 1.17343 0.936 11 150.00 24.00 15.35 1.17608 144.867 1.1708 0.936 12 150.27 24.00 15.35 1.17808 144.867 1.1708 0.936 13 150.00 21.37 16.23 1.21852 138.854 1.20722 0.928 14 180.00 23.28 14.00 1.19986 139.042 1.12211 0.923 15 180.00 22.57 14.00 1.21949 133.218 1.20123 0.920	I XI Point Prediction	6	150.00	20.02	16.99	1.02972	143.148	1.18007	0.946			
8 150.00 20.00 16.94 1.03001 143.332 1.17254 0.945 9 150.00 20.05 16.93 1.03875 142.913 1.17657 0.945 10 150.00 24.00 15.35 1.17862 144.999 1.17343 0.936 11 150.00 24.00 15.35 1.17868 144.867 1.16995 0.936 12 150.27 24.00 15.35 1.17808 144.867 1.1708 0.936 13 150.00 21.37 16.23 1.21852 136.854 1.20722 0.928 14 180.00 23.28 14.00 1.10988 139.042 1.12211 0.923 16 180.00 22.57 14.00 1.21949 133.218 1.20123 0.920		7	150.67	20.12	17.00	1.04597	142.003	1.18845	0.945			
9 150.00 20.05 16.93 1.03875 142.913 1.17657 0.945 10 150.00 24.00 15.35 1.17862 144.999 1.17343 0.936 11 150.00 24.00 15.35 1.17687 1.995 0.936 12 150.27 24.00 15.35 1.17808 144.867 1.1708 0.936 13 150.00 21.37 16.23 1.21852 136.854 1.20722 0.928 14 180.00 23.28 14.00 1.1988 139.042 1.12211 0.923 16 180.00 22.57 14.00 1.21949 133.218 1.20123 0.920		8	150.00	20.00	16.94	1.03001	143.332	1.17254	0.945			
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Report 11 150.00 24.00 15.33 1.17548 145.324 1.16995 0.936 12 150.27 24.00 15.35 1.17008 144.867 1.1708 0.936 13 150.00 21.37 16.23 1.21852 136.854 1.20722 0.928 14 180.00 23.09 14.00 1.13934 137.463 1.14337 0.924 15 180.00 22.57 14.00 1.21949 133.218 1.20123 0.920		10	150.00	24.00	15.35	1.17862	144.999	1.17343	0.936			
Item 12 150.27 24.00 15.35 1.17808 144.867 1.1708 0.936 13 150.00 21.37 16.23 1.21852 136.854 1.20722 0.928 14 180.00 23.09 14.00 1.13934 137.463 1.14337 0.924 15 180.00 22.57 14.00 1.10988 139.042 1.12211 0.923 16 180.00 22.57 14.00 1.21949 133.218 1.20123 0.920	Report	11	150.00	24.00	15.33	1.17548	145.324	1.16995	0.936			
13 150.00 21.37 16.23 1.21852 136.854 1.20722 0.928 14 180.00 23.09 14.00 1.13934 137.463 1.14337 0.924 15 180.00 23.28 14.00 1.10988 139.042 1.12211 0.923 16 180.00 22.57 14.00 1.21949 133.218 1.20123 0.920	Bar Graph	12	150.27	24.00	15.35	1.17808	144.867	1.1708	0.936			
14 180.00 23.09 14.00 1.13934 137.463 1.14337 0.924 15 180.00 23.28 14.00 1.10988 139.042 1.12211 0.923 16 180.00 22.57 14.00 1.21949 133.218 1.20123 0.920		13	150.00	21.37	16.23	1.21852	136.854	1.20722	0.928			
15 180.00 23.28 14.00 1.10988 139.042 1.12211 0.923 16 180.00 22.57 14.00 1.21949 133.218 1.20123 0.920		14	180.00	23.09	14.00	1.13934	137.463	1.14337	0.924			
16 180.00 22.57 14.00 1.21949 133.218 1.20123 0.920		15	180.00	23.28	14.00	1.10988	139.042	1.12211	0.923			
		16	180.00	22.57	14.00	1.21949	133.218	1.20123	0.920			
16 Solutions found		16 Solutions fou	nd									

Figure 25: Optimal solutions of numerical optimization model

From the results of Table 25, it was observed that a current of 150amp, voltage of 20volts and gas flow rate of 17.00L/min will produce a weld material with Kinematic Viscosity of 1.17915x10-6m2/s .This solution was selected by design expert as the optimal solution with a desirability value of 94.60%.

The desirability bar graph which shows the accuracy with which the model is able to predict the values of the selected input variables and the corresponding responses is presented in Figure 26.



Figure 26: Prediction accuracy of numerical optimzation

It can be deduce from the result of Figure 4.52 that the model developed based on response surface methodology and optimized using numerical optimization method, predicted the Kinematic Viscosity with an accuracy level of 90.08%

The contour plots showing kinematic viscosity variable against the optimized value of the input variable is presented in Figure 27



Figure 27: Predicting kinematic viscosity using contour plot Figure 28: Predicting desirability using contour plot

A plot of desirability against the input variables is presented in figure 28. As presented in Figures 28, the contour plot can be employed to predict the optimum values of the input variables based on the flagged response variables.

Conclusion

In this study, the response surface methodology was used to optimize the molten, metal properties such as Kinematic viscosity of gas tungsten arc mild steel welds. The Result revealed that the model is of the quadratic type which requires the polynomial analysis order as depicted by a typical response surface design. Coefficient of determination R2 values of 0.9603 kinematic viscosity model. Adeq Precision measures the signal to noise ratioof19.260which indicates adequate signal. From the results, it was observed that a current of 150.00 Amp, voltage of 20 volt and a gas flow rate of 17 L/min will produce a welded material having kinematic viscosity of 1.179 at a desirability of 0.946. Response surface methodology using numerical optimization was effective in predicting the kinematic viscosity.

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